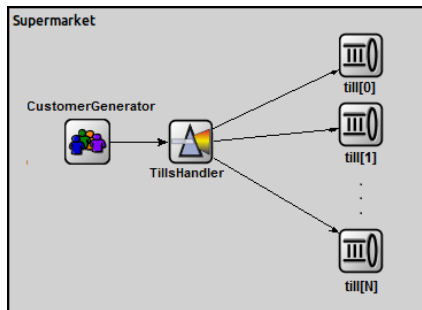


## Project 2 - Quick Checkout

Francesco Paolo Culcasi  
Alessandro Martinelli  
Nicola Messina

M. Sc. in Computer Engineering  
Performance Evaluation of Computer System and Network

- 1 Model
  - System Description and Implementation
  - Verification and Calibration
- 2 Analysis
  - Scenario Definitions
  - Exponential Service Demand
  - Lognormal Service Demand
- 3 Theoretical Result Analysis
  - Model Fitting attempts



- Project assumptions
  - Inter-arrival and Service demand
  - Splitting policy
  - Quick checkout tills
  - Service time
- Modeling and Implementation
  - CustomerGenerator
  - Customer
  - TillsHandler
  - Till

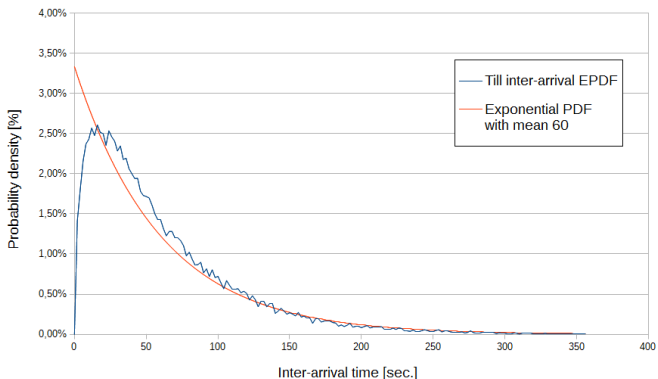
## System verification

- Varying  $P$
- Varying  $SD$
- Constant  $IA$

$$SD = \frac{IA \cdot N}{unitServiceTime}$$

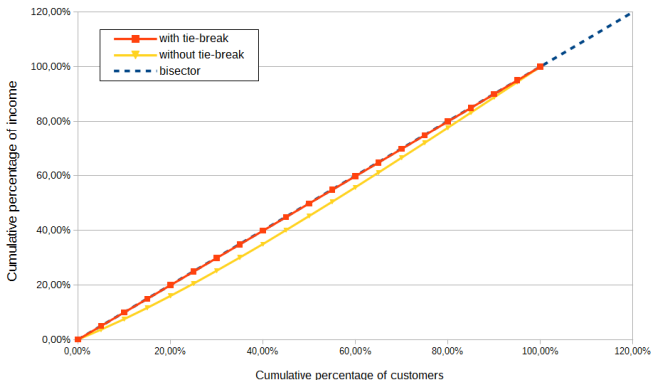
## Calibration

- Comparison with M/M/1 system
- Parameters with fixed values, i.e.  $N = 20$ ,  $unitServiceTime = 2s$ .
- Significant values for  $K$  and  $P$

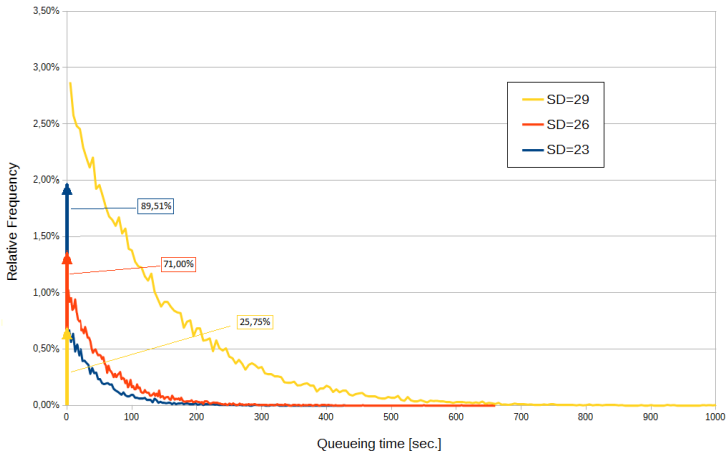


	Exponential SD		Lognormal SD
Undistinguished tills	$P=0$ , exp SD		$P=0$ , logn SD
	↕		↕
Normal & Quick checkout tills	$P=0.1$ , exp SD	↔	$P=0.1$ , logn SD

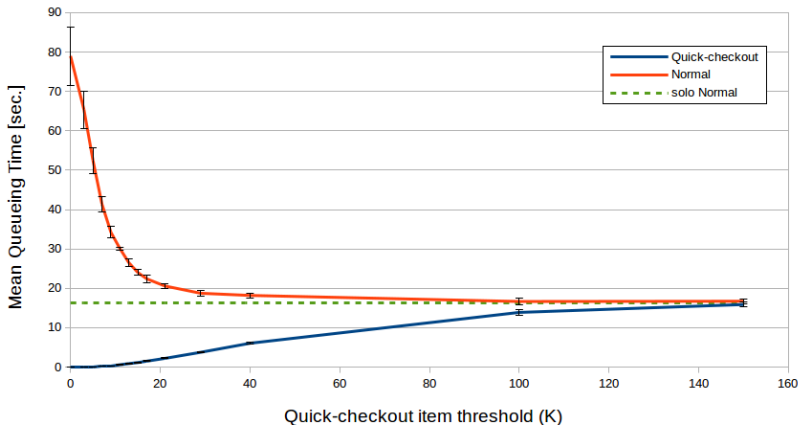
- Warm-up time analysis
- Load fairly distributed



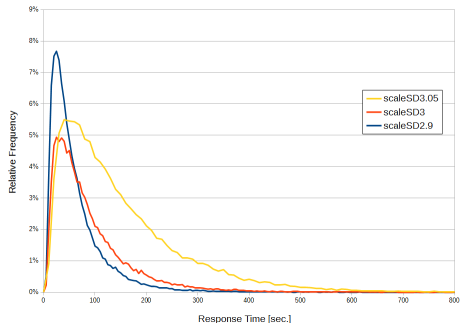
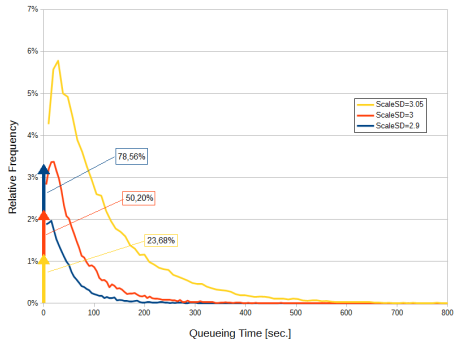
- IA at a single queue is not exponential
- QT increasing with SD and has a Delta in 0.
- This is not a PASTA system, since  $p_0 \neq r_0$



- Quick-Checkout tills behavior varying K
- Normal tills behavior varying K.
- Same trend: Solo Normal queueing time.



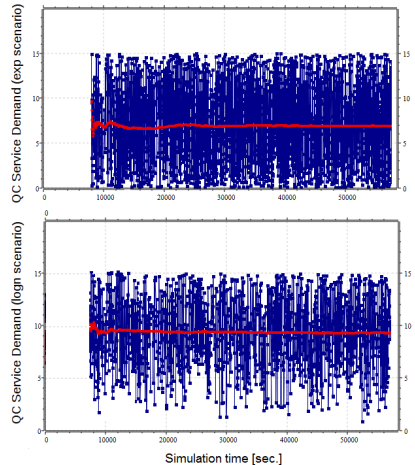
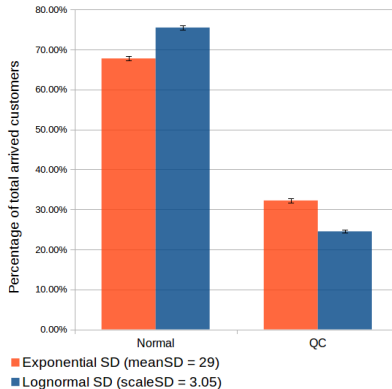
- Comparison with *Exp Undistinguished Tills*
  - ⇒ Similar behaviour
  - ⇒ Lower probability to obtain lower queueing times
- Difference among QT and RT distributions





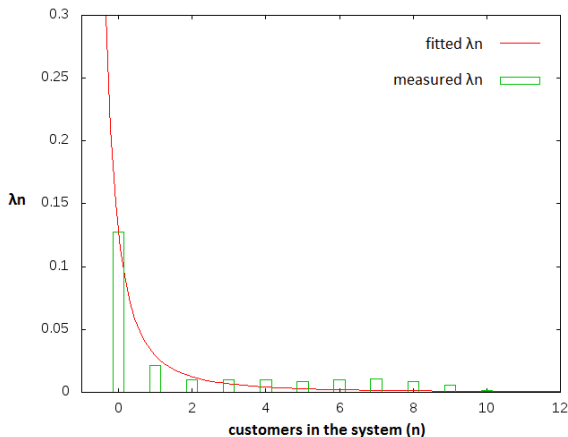
## Differences over *Exp Normal+Quick checkout*:

- Higher mean service demand of quick checkout customers
  - ⇒ Lower load (totArrivedCustomers)
  - ⇒ Higher idle time



- Customers are sent to tills relying on the # of customers in each of them (NON probabilistic splitting). This brings to state dependent arrival rates.  
⇒ Tills are non M/M/1 systems
- We can still use M/M/1 as an overestimation of the mean # of customers in the till
- We have a closed form for  $E[N]$

- Till arrival rate ( $\lambda_n$ ) looks like a hyperbole, leading the analysis to hypothesize it is a standard discouraged model
- Actually a discouraged model variation fits lot better.



$$\lambda_n = \frac{\lambda}{(n+1)^\alpha}$$
$$\alpha \simeq 2$$

- Using Chapman-Kolmogorov equations we can exploit  $E[N]$  in a closed form
- both M/M/1 system and our system loads can be compared

$$E[n] = \frac{\sum_{n=0}^{\infty} \frac{n \cdot \left(\frac{\lambda}{\mu}\right)^n}{(n!)^2}}{\sum_{k=0}^{\infty} \frac{\left(\frac{\lambda}{\mu}\right)^k}{(k!)^2}} = \frac{\sqrt{\frac{\lambda}{\mu}} I_1\left(2\sqrt{\frac{\lambda}{\mu}}\right)}{I_0\left(2\sqrt{\frac{\lambda}{\mu}}\right)}$$

